

DOE PRACTICE PAPER – 1 (TERM – 1) (SESSION 2021 – 22)

CLASS XII

MATHEMATICS (CODE: 041)

Time Allowed: 90 Minutes

Maximum Marks: 40

General Instructions:

1. This question paper contains **three sections – A, B and C**. Each part is compulsory.
2. **Section - A** has **20 MCQs**, **attempt any 16 out of 20**.
3. **Section - B** has **20 MCQs**, **attempt any 16 out of 20**.
4. **Section - C** has **10 MCQs**, **attempt any 8 out of 10**.
5. There is **no negative marking**.
6. All questions carry equal marks.

SECTION – A In this section, attempt any 16 questions out of Questions 1 – 20. Each question is of 1 mark weightage. Each MCQ has four options with only one correct option, choose the correct option.		
1.	The range of the function $f(x) = \tan^{-1} x + \cot^{-1} x$ is (a) $[-\frac{\pi}{2}, \frac{\pi}{2}]$ (b) $[0, \pi]$ (c) $[0, \frac{\pi}{2}]$ (d) $\{\frac{\pi}{2}\}$	1
2.	The value of the expression $\sec^{-1}(2) + \sin^{-1}(\frac{1}{2}) + \tan^{-1}(-\sqrt{3})$ is (a) $\frac{5\pi}{6}$ (b) $\frac{\pi}{3}$ (c) $\frac{-\pi}{3}$ (d) $\frac{\pi}{6}$	1
3.	The relation R in the set {a, b, c} given by $R = \{(a, a), (b, b), (a, b), (b, a)\}$ is (a) symmetric and transitive, but not reflexive (b) reflexive and symmetric, but not transitive (c) symmetric, but neither reflexive nor transitive (d) an equivalence relation	1
4.	$A = \{1, 2, 3, 4\}$, A relation R in the set A is given by $R = \{(1, 1), (2, 3), (3, 2), (4, 3), (3, 4)\}$, then relation R is (a) Reflexive (b) symmetric (c) Transitive (d) Equivalence	1
5.	If A is any square matrix of order 3×3 such that $ \text{adj } A = 256$, then the sum of all possible values of $ A $ is (a) 256 (b) 16 (c) – 16 (d) 0	1

6.	If $\begin{bmatrix} x-2 & 5+y \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} = O$, Then $x + y =$ (a) 0 (b) -2 (c) -1 (d) -3	1
7.	If A is a diagonal matrix of order 3×3 such that $A^2 = A$, then number of possible matrices A are (a) 4 (b) 8 (c) 16 (d) 32	1
8.	If $\begin{bmatrix} 1 & -1 \\ 2 & 3 \end{bmatrix} + X = \begin{bmatrix} 3 & 4 \\ 5 & 6 \end{bmatrix}$, where $X = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$, Then $a + c - b - d =$ (a) 13 (b) 5 (c) -8 (d) -3	1
9.	If A is a symmetric matrix then which of the following is not Symmetric matrix, (a) $A + A^T$ (b) $A.A^T$ (c) $A - A^T$ (d) A^T	1
10.	If A is a non-singular square matrix of order 3 such that $ A = 3$, then value of $ 2A^T $ is (a) 3 (b) 6 (c) 12 (d) 24	1
11.	If $y = \frac{1}{1+x^{b-a}+x^{c-a}} + \frac{1}{1+x^{c-b}+x^{a-b}} + \frac{1}{1+x^{a-c}+x^{b-c}}$, then $\frac{dy}{dx} =$ (a) x^{a+b+c} (b) x^{abc} (c) $\frac{1}{x^a+x^b+x^c}$ (d) 0	1
12.	Suppose P, Q and R are different matrices of order 3×5 , $a \times b$ and $c \times d$ respectively, then value of $ac + bd$ is, if matrix $2P + 3Q - 4R$ is defined (a) 9 (b) 30 (c) 34 (d) 15	1
13.	The function given below at $x = 4$ is $f(x) = \begin{cases} 2x+3, & x \leq 4 \\ x^2-5, & x > 4 \end{cases}$ (a) Continuous but not differentiable (b) Differentiable but not continuous (c) Continuous as well as differentiable (d) Neither continuous nor differentiable	1
14.	If $x^3 - 3x^2y + y^3 = 2021 + xy$ then $\frac{dy}{dx} =$ (a) $\frac{3x^2 - 6xy - y}{3x^2 + 3y^2 - x}$ (b) $\frac{3x^2 - 6xy - y}{3y^2 - 3x^2 - x}$ (c) $\frac{6xy + y - 3x^2}{3y^2 - 3x^2 - x}$ (d) $\frac{3x^2 - 6xy - y}{3x^2 + 3y^2 + x}$	1

15.	The slope of the tangent to the curve $y = x^3$, at the point (2, 8) is (a) 2 (b) 6 (c) 11 (d) 12	1
16.	Corner points of the feasible region determined by the system of linear constraints are (0, 3), (1, 1) and (3, 0). Let $Z = px + qy$, where $p, q > 0$. Condition on p and q so that the minimum of Z occurs at (3, 0) and (1, 1) is (a) $p = 2q$ (b) $q = 2p$ (c) $p = 3q$ (d) $p = q$	1
17.	The points on the curve $4x^2 + 9y^2 = 36$ at which tangent to the curve is parallel to x-axis, is (a) $(\pm 2, 0)$ (b) $(0, \pm 2)$ (c) $(0, \pm 3)$ (d) $(\pm 3, 0)$	1
18.	The interval in which $y = -x^3 + 3x^2 + 2021$ is increasing is (a) $(-\infty, \infty)$ (b) $(0, 2)$ (c) $(2, \infty)$ (d) $(-2, 0)$	1
19.	If $x = \log_e y$, then $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} =$ (a) y (b) 2y (c) $-2y$ (d) $-y$	1
20.	If $x = \sin^3 t$, $y = \cos^3 t$ then $\frac{dy}{dx} =$ (a) $\tan t$ (b) $\cot t$ (c) $-\tan t$ (d) $-\cot t$	1

SECTION – B

In this section, attempt any 16 questions out of Questions 21 – 40.

Each question is of 1 mark weightage.

Each MCQ has four options with only one correct option, choose the correct option.

21.	If $\sin^{-1} x + \sin^{-1} y = \frac{2\pi}{3}$, $\cos^{-1} x + \cos^{-1} y =$ (a) $\frac{-\pi}{3}$ (b) $\frac{\pi}{3}$ (c) π (d) $\frac{\pi}{2}$	1
22.	Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be defined as $f(x) = 7x - 5$, then (a) f is one-one onto (b) f is many-one onto (c) f is one-one but not onto (d) f is neither one-one nor onto	1
23.	A relation R in the set of real numbers R is given by $R = \{(a, b) : a > b, a, b \in \mathbb{R}\}$, The relation R is (a) Reflexive (b) symmetric (c) Transitive (d) Equivalence	1
24.	If $a \leq 2\sin^{-1} x + \cos^{-1} x \leq b$, then (a) $a = 0, b = \pi$ (b) $a = \pi, b = 2\pi$ (c) $a = \frac{-\pi}{2}, b = \frac{\pi}{2}$ (d) $a = 0, b = \frac{\pi}{2}$	1

25.	If $A^{-1} = \begin{bmatrix} 3 & 1 & 2 \\ 0 & 1 & 2 \\ 0 & 2 & 1 \end{bmatrix}$, then $adjA =$ (a) $\frac{1}{9}$ (b) $\frac{1}{81}$ (c) -9 (d) -81	1
26.	If A and B are two square matrices of same order such that, $AB = A$ and $BA = B$, then $(A + B)(A - B) =$ (a) $A^2 - B^2$ (b) $2A - 2B$ (c) $2A + 2B$ (d) O	1
27.	If $5^x + 5^y = 5^{x+y}$, then $\frac{dy}{dx} =$ (a) 5^{x-y} (b) 5^{y-x} (c) -5^{x-y} (d) -5^{y-x}	1
28.	The interval on which the function $f(x) = 2x^3 - 3x^2 - 36x + 10$ is decreasing is (a) $(-\infty, -2)$ (b) $(-2, 3)$ (c) $(2, 3)$ (d) $(3, \infty)$	1
29.	If the curve $ay + x^2 = 7$ and $x^3 = y$, cut orthogonally at $(1, 1)$, then the value of a is: (a) 1 (b) 3 (c) -6 (d) 6	1
30.	If $\log\left(\frac{x^2 - y^2}{x^2 + y^2}\right) = a$, then $\frac{dy}{dx} =$ (a) $\frac{y}{x}$ (b) $\frac{-y}{x}$ (c) $\frac{x}{y}$ (d) $\frac{-x}{y}$	1
31.	The area of a triangle with vertices $(-3, 0)$, $(3, 0)$ & $(0, k)$ is 9 sq. units. The value of k is ($k > 0$) (a) 3 (b) 6 (c) 9 (d) 12	1
32.	If $\begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ 3 \\ 2 \end{bmatrix}$, then $2x + y - z =$ (a) 2 (b) 1 (c) 3 (d) 5	1
33.	If $\tan y = x$, then when $x = 1$, value of $4 \frac{d^2y}{dx^2}$ is (a) 2 (b) -2 (c) 1 (d) -1	1
34.	If a non-singular Matrix A satisfy $2A^2 + A - I = O$, then $A^{-1} =$ (a) $2A - I$ (b) $2A + I$ (c) $4A + 2I$ (d) $2A - 4I$	1
35.	The maximum value of the function $f(x) = 4 \sin x \cos x$ is (a) 2 (b) 4 (c) 1 (d) 8	1

36.	If the objective function $z = ax + y$ is minimum at $(1, 4)$ and its minimum value is 13, then value of a is (a) 1 (b) 4 (c) 9 (d) 13	1
37.	Let L be the set of all lines in a plane. A relation R in L is given by $R = \{(L_1, L_2) : L_1 \text{ and } L_2 \text{ intersect at exactly one point, } L_1, L_2 \in L\}$, then the relation R is (a) Reflexive (b) Symmetric (c) Transitive (d) Equivalence	1
38.	If $f : X \rightarrow Y$ is defined, then f is <pre> graph LR subgraph X 1 2 3 4 end subgraph Y a b c d end 1 --> a 2 --> b 3 --> c 4 --> c </pre> (a) Bijective function (b) Many-one and onto (c) Many-one and Into function (d) One-one but not onto	1
39.	The feasible region for an LPP is always a _____ polygon (a) Convex (b) Concave (c) either (a) or (b) (d) neither (a) nor (b)	1
40.	The tangent to the curve $y = e^x$ at the point $(0, 1)$ meets x -axis at (a) $(1, 0)$ (b) $(-1, 0)$ (c) $(0, 0)$ (d) $(2, 0)$	1

SECTION – C

In this section, attempt any 8 questions out of Questions 41 – 50.

Each question is of 1 mark weightage.

Each MCQ has four options with only one correct option, choose the correct option.

Questions 46-50 are based on a Case-Study

41.	The feasible region, for the inequalities $x + 2y \leq 6$, $y \geq 0$, $0 \leq x$ lies in (a) First Quadrant (b) Second Quadrant (c) Third Quadrant (d) Fourth Quadrant	1
42.	Which of the following function is decreasing on $(0, \frac{\pi}{2})$ (a) $\sin x$ (b) $\cos x$ (c) $\tan x$ (d) $\sin 2x$	1
43.	If the function $f(x) = \sin x - ax + b$, is decreasing on $x \in \mathbb{R}$, then a belongs to (a) $(1, \infty)$ (b) $[0, \infty)$ (c) $(0, \infty)$ (d) $[1, \infty)$	1
44.	In a linear programming problem, If the feasible region is bounded then objective function $Z = px + qy$ has (a) Maximum value only (b) Minimum value only (c) Maximum and minimum value both (d) Neither maximum nor minimum value	1
45.	If $A = \begin{bmatrix} 6x & 8 \\ 3 & 2 \end{bmatrix}$ is singular matrix, then the value of x is (a) 3 (b) -2 (c) 0 (d) 2	1

CASE STUDY

The fuel cost per hour for running a train is proportional to the square of the speed it generates in km per hour. If the fuel costs ₹ 48 per hour at speed 16 km per hour and the fixed charges to run the train amount to ₹ 1200 per hour.

Assume the speed of the train as v km/h.



Based on the given information, answer the following questions.

46.	Given that the fuel cost per hour is k times the square of the speed the train generates in km/h, the value of $16k$ is: (a) 1 (b) 2 (c) 3 (d) 4	1
47.	If the train has travelled a distance of 1000 km, then the total cost of running the train is given by function: (a) $\frac{375}{4}v + \frac{60000}{v}$ (b) $\frac{375}{8}v + \frac{60000}{v}$ (c) $\frac{375}{2}v + \frac{60000}{v}$ (d) $\frac{375}{2}v + \frac{1200000}{v}$	1
48.	The most economical speed to run the train (in Km/hr) is: (a) 50 (b) 80 (c) 400 (d) 800	1
49.	The fuel cost (In Rs.) for the train to travel 1000km at the most economical speed is: (a) 15000 (b) 75000 (c) 100000 (d) 150000	1
50.	The total cost of the train to travel 1000km at the most economical speed is: (a) 15000 (b) 30000 (c) 100000 (d) 150000	1